Lecture 2

Introduction to Data Flow Analysis

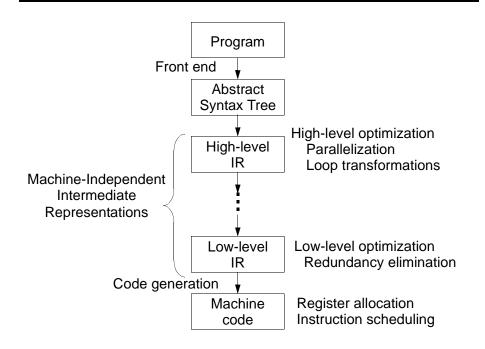
- I Introduction
- II Example: Reaching definition analysis
- III Example: Liveness Analysis
- IV A General Framework (Theory in next lecture)

Reading: Chapter 9.2

Advanced Compilers

M. Lam

I. Compiler Organization



- Basic block = a maximal sequence of consecutive instructions s.t.
 - flow of control only enters at the beginning
 - flow of control can only leave at the end (no halting or branching except perhaps at end of block)

• Flow Graphs

- · Nodes: basic blocks
- Edges
 - $B_i \rightarrow B_i$, iff B_i can follow B_i immediately in some execution

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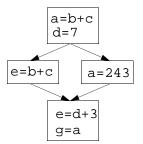
What is Data Flow Analysis?

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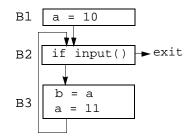
- Data flow analysis:
 - · Flow-sensitive: sensitive to the control flow in a function

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- intraprocedural analysis
- Examples of optimizations:
 - Constant propagation
 - · Common subexpression elimination
 - Dead code elimination



Value of x? Which "definition" defines x? Is the definition still meaningful (live)?

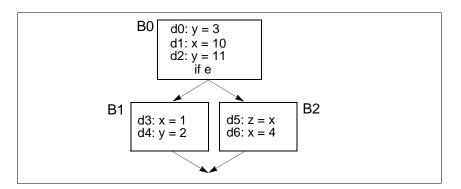


- Statically: Finite program
- Dynamically: Can have infinitely many possible execution paths
- Data flow analysis abstraction:
 - For each **static** point in the program: combines information of all the **dynamic** instances of the same program point.
- Example of a data flow question:
 - Which definition defines the value used in statement "b = a"?

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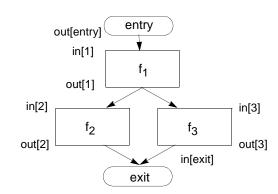
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II. Reaching Definitions



- Every assignment is a definition
- A definition *d* reaches a point *p* if there exists a path from the point immediately following *d* to *p* such that *d* is not killed (overwritten) along that path.
- Problem statement
 - For each point in the program, determine if each definition in the program reaches the point
 - A bit vector per program point, vector-length = #defs

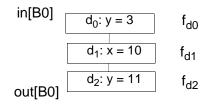
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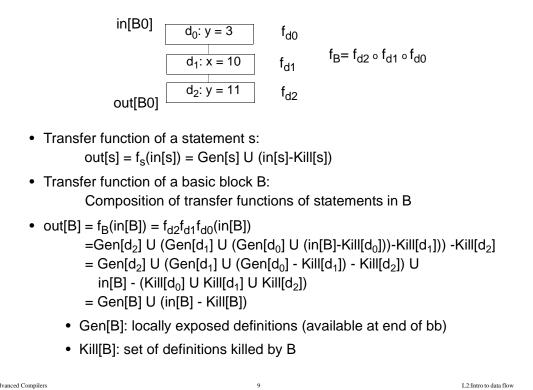
- Build a flow graph (nodes = basic blocks, edges = control flow)
- Set up a set of equations between in[b] and out[b] for all basic blocks b
 - Effect of code in basic block: Transfer function f_b relates in[b] and out[b], for same b
 - Effect of flow of control: relates out[b₁], in[b₂] if b₁ and b₂ are adjacent
- · Find a solution to the equations

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Effects of a Statement

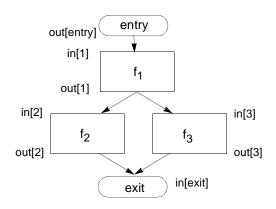


- f_s : A transfer function of a statement abstracts the execution with respect to the problem of interest
- For a statement s (d: x = y + z) out[s] = f_s(in[s]) = Gen[s] U (in[s]-Kill[s])
 - **Gen[s]:** definitions generated: Gen[s] = {d}
 - Propagated definitions: in[s] Kill[s], where Kill[s]=set of all other defs to x in the rest of program



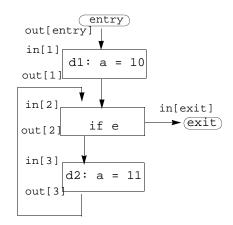
Effects of the Edges (acyclic)

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· Join node: a node with multiple predecessors

meet operator (
$$\land$$
): \cup
in[b] = out[p₁] \cup out[p₂] $\cup ... \cup$ out[p_n], where
p₁, ..., p_n are predecessors of b



- Equations still hold
 - $out[b] = f_b(in[b])$
 - in[b] = out[p₁] \cup out[p₂] $\cup ... \cup$ out[p_n], p₁, ..., p_n pred.
- Find: fixed point solution

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Reaching Definitions: Iterative Algorithm

```
input: control flow graph CFG = (N, E, Entry, Exit)
// Boundary condition
OUT[Entry] = Ø
// Initialization for iterative algorithm
For each basic block B other than Entry
OUT[B] = Ø
// iterate
While (changes to any OUT occur) {
    For each basic block B other than Entry {
        in[B] = ∪ (out[p]), for all predecessors p of B
        out[B] = f<sub>B</sub>(in[B]) // out[B]=gen[B]∪(in[B]-kill[B])
    }
```

	Reaching Definitions	
Domain	Sets of definitions	
Transfer function f _b (x)	forward: out[b] = $f_b(in[b])$ $f_b(x) = Gen_b \cup (x \text{-Kill}_b)$	
	Gen _b : definitions in b	
	Kill _b : killed defs	
Meet Operation	in[b]= \cup out[predecessors]	
Boundary Condition	out[entry] = Ø	
Initial interior points	out[b] = Ø	

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III. Live Variable Analysis

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• Definition

- A variable v is live at point p if the value of v is used along some path in the flow graph starting at p.
- Otherwise, the variable is **dead**.

• Problem statement

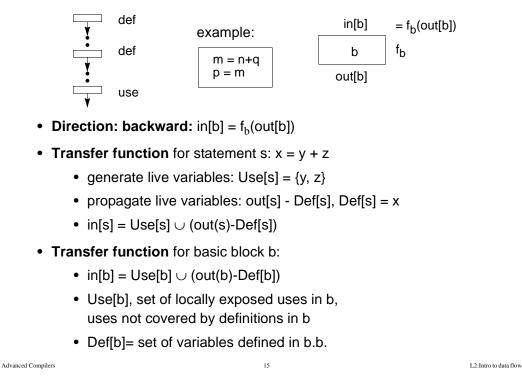
- For each basic block b,
 - determine if each variable is live at the start/end point of b

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• Size of bit vector: one bit for each variable

Effects of a Basic Block (Transfer Function)

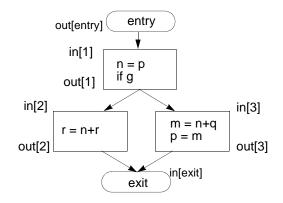
• Observation:Trace uses back to the definitions



Across Basic Blocks

- Meet operator (<):
 - out[b] = in[s₁] \cup in[s₂] \cup ... \cup in[s_n], s₁, ..., s_n are successors of b
- Boundary condition:

Example



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Liveness: Iterative Algorithm

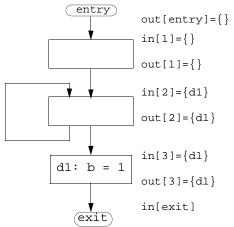
```
input: control flow graph CFG = (N, E, Entry, Exit)
// Boundary condition
IN[Exit] = Ø
// Initialization for iterative algorithm
For each basic block B other than Exit
IN[B] = Ø
// iterate
While (changes to any IN occur) {
   For each basic block B other than Exit {
      out[B] = ∪ (in[s]), for all successors of B
      in[B] = f_B(out[B]) // in[B]=Use[B]∪(out[B]-Def[B])
   }
```

	Reaching Definitions	Live Variables
Domain	Sets of definitions	Sets of variables
Direction	forward: $out[b] = f_b(in[b])$ $in[b] = \land out[pred(b)]$	backward: in[b] = f _b (out[b]) out[b] = ∧ in[succ(b)]
Transfer function	$f_b(x) = Gen_b \cup (x \text{-}Kill_b)$	$f_b(x) = Use_b \cup (x \operatorname{-Def}_b)$
Meet Operator (^)	U	U
Boundary Condi- tion	out[entry] = Ø	$in[exit] = \emptyset$
Initial Interior points	out[b] = Ø	in[b] = Ø

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Thought Problem 1. "Must-Reach" Definitions

- A definition D (a = b+c) <u>must</u> reach point P iff
 - D appears at least once along on all paths leading to P
 - a is not redefined along any path after last appearance of D and before P
- How do we formulate the data flow algorithm for this problem?



Problem 2: A legal solution to (May) Reaching Def?

• Will the worklist algorithm generate this answer?

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Problem 3. What are the algorithm properties?

- Correctness
- Precision: how good is the answer?
- Convergence: will the analysis terminate?
- Speed: how long does it take?