### 2.4 HEAPSORT DEMO


click to begin demo

Heapsort

Starting point. Array in arbitrary order.
we assume array entries are indexed 1 to N


| $\mathbf{S}$ | O | R | T | E | X | A | M | P | L | E |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |

Heapsort

Heap construction. Build max heap using bottom-up method.


| S | O | R | T | E | X | A | M | P | L | E |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 6 | 7 | 8 | 9 | 10 | 11 |  |  |  |  |  |

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 5


5

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 5


Heapsort

Heap construction. Build max heap using bottom-up method.
sink 5

S O
R
L
x
A
M
E E

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 4


Heapsort

Heap construction. Build max heap using bottom-up method.
sink 4


$$
\begin{array}{l|l|l|l|l|l|l|l|l}
\mathrm{S} & \mathrm{O} & \mathrm{R} & \mathrm{~T} & \mathrm{~L} & \mathrm{X} & \mathrm{~A} & \mathrm{M} & \mathrm{P} \\
\hline
\end{array}
$$

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 3


3

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 3


Heapsort

Heap construction. Build max heap using bottom-up method.
sink 3


$$
\begin{array}{l|l|l|l|l|l|l|l|l}
\hline S & O & X & T & L & A & A & M & P \\
\hline
\end{array}
$$

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 2

$\begin{array}{ll}\mathrm{S} & \mathrm{O} \\ & 2\end{array}$

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 2


| S | T | X | O | $L$ | $R$ | $A$ | $M$ | $P$ | $E$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 2


| S | T | X | P | L | R | A | M | O | E | E |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2 |  | 4 |  |  |  |  | 9 |  |  |

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 2


$$
\begin{array}{l|llllllllll}
\text { S } & \mathrm{T} & \mathrm{X} & \mathrm{P} & \mathrm{~L} & \mathrm{R} & \mathrm{~A} & \mathrm{M} & \mathrm{O} & \mathrm{E} & \mathrm{E} \\
\hline
\end{array}
$$

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 1


$$
\begin{array}{l|l|l|l|l|l|l|l|l|l|l}
\hline \text { S } & \text { T } & \text { X } & \text { P } & \text { L } & \text { R } & \text { A } & \text { M } & \text { O } & \text { E } & \text { E } \\
\hline 1 & & & & & & & & &
\end{array}
$$

Heapsort

Heap construction. Build max heap using bottom-up method.
sink 1


$$
\begin{array}{llllllllllll}
\mathrm{X} & \mathrm{~T} & \mathrm{~S} & \mathrm{P} & \mathrm{~L} & \mathrm{R} & \mathrm{~A} & \mathrm{M} & \mathrm{O} & \mathrm{E} & \mathrm{E} \\
\hline 1 & & 3 & & & & & & & &
\end{array}
$$

Heapsort

Heap construction. Build max heap using bottom-up method.
end of construction phase
11 -node heap


$$
\begin{array}{l|l|l|l|l|l|l|l|l|l}
\hline X & T & S & P & L & R & A & M & O & E
\end{array}
$$

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## exchange 1 and 11



| $X$ | T | S | P | L | R | A | M | O | E | E |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |  |  |  |  |  | 11 |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 11


| E | T | S | P | L | R | A | M | O | E | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |  |  |  |  |  | 11 |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



$$
\begin{array}{l|l|l|l|l|l|l|l|l|l}
\hline \text { T } & \mathrm{E} & \mathrm{~S} & \mathrm{P} & \mathrm{~L} & \mathrm{R} & \mathrm{~A} & \mathrm{M} & \mathrm{O} & \mathrm{E}
\end{array} \mathrm{X}
$$

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| T | P | S | E | L | R | A | M | O | E | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 |  | 4 |  |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| T | P | S | O | L | R | A | M | E | E | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 |  | 4 |  |  |  |  | 9 |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.


$$
\begin{array}{l|l|l|l|l|l|l|l|l|l}
\hline \text { T } & \mathrm{P} & \mathrm{~S} & \mathrm{O} & \mathrm{~L} & \mathrm{R} & \mathrm{~A} & \mathrm{M} & \mathrm{E} & \mathrm{E}
\end{array} \mathrm{X}
$$

Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 10


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 10


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| E | P | S | O | L | R | A | M | E | T | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| S | P | E | O | L | R | A | M | E | T | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  | 3 |  |  |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| $S$ | $P$ | $R$ | $O$ | $L$ | $E$ | A | M | E | T | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  | 3 |  |  | 6 |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.


$$
\begin{array}{l|l|l|l|l|l|l|l|l|l|l}
\hline \text { S } & \mathrm{P} & \mathrm{R} & \mathrm{O} & \mathrm{~L} & \mathrm{E} & \mathrm{~A} & \mathrm{M} & \mathrm{E} & \mathrm{~T} & \mathrm{X}
\end{array}
$$

Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 9


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 9


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| $R$ | $P$ | $E$ | $O$ | $L$ | $E$ | A | M | S | T | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  | 3 |  |  |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 8


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 8


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| $P$ | $M$ | $E$ | O | L | E | A | R | S | T | X |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 |  |  |  |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



| P | O | E | M | L | E | A | R | S | T |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | 2 |  | 4 |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 7


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 7


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## sink 1



$$
\begin{array}{l|l|l|l|l|l|l|l|l}
\mathrm{O} & \text { M } & \mathrm{E} & \mathrm{~A} & \mathrm{~L} & \mathrm{E} & \mathrm{P} & \mathrm{R} & \mathrm{~S} \\
\hline
\end{array}
$$

Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 6


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 6


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## exchange 1 and 5



| M | L | E | A | E | O | P | R | S | T | X |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  | 5 |  |  |  |  |  |  |

Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## exchange 1 and 5



P


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 4


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 4


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.

## exchange 1 and 3



Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 3


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
sink 1


Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 2


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
exchange 1 and 2


Heapsort

Sortdown. Repeatedly delete the largest remaining item.


Heapsort

Sortdown. Repeatedly delete the largest remaining item.
end of sortdown phase


Heapsort

Ending point. Array in sorted order.


